# Voltage-Biased High-T<sub>c</sub> Superconducting Infrared Bolometers with Strong Electrothermal Feedback

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Abstract — In the current generation of high-T<sub>c</sub> bolometers the thermal conductance is often chosen for a short time-constant rather than for sensitivity. We describe optimal bolometer bias and readout scheme that promises to relax this constraint. Voltage bias of the superconductor results in strong electrothermal feedback that greatly reduces the time-constant of the bolometer. We estimate that a decrease of more than one order of magnitude in time-constant should be possible with existing high-T<sub>c</sub> thermometers. We give theoretical estimates of the performance gain with voltage bias for several bolometers that have been reported in the literature. We find cases where the sensitivity can be greatly improved (by changing the thermal conductance) while holding the time constant fixed and others where the bolometer can be made much faster while maintaining the sensitivity.

# I. INTRODUCTION

Infrared bolometers with high-T<sub>c</sub> superconducting thermometers can be more than an order of magnitude more sensitive than other liquid-nitrogen-cooled (or room temperature) technologies at wavelengths longer than 10 µm. Existing liquid-nitrogen-cooled photon detectors lose sensitivity at long wavelengths because of thermally-excited dark current. Applications of high-T<sub>c</sub> bolometers include infrared spectroscopy[1] and space-based observations of bright sources such as planets[3]. In particular, arrays of high-T<sub>c</sub> bolometers are very attractive for imaging at wavelengths longer than 10 µm.[4]

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Superconducting transition-edge bolometers have traditionally been operated with a constant-current bias, which results in positive electrothermal feedback (ETF).[5] The bias current must therefore be limited to avoid thermal instability. It has recently been pointed out[6] that a constant-voltage bias mode with strong negative ETF[6,7] gives several important operational advantages. The most important of these is a large reduction of the bolometer time-constant due to strong ETF. We estimate a decrease of more than one order of magnitude in time constant should be possible with existing high-T<sub>C</sub> thermometers.

In the current generation of high- $T_{\text{C}}$  bolometers the thermal conductance is often chosen for a short time-constant rather than for optimal sensitivity. The time-constant decrease due to negative ETF can be used to relax this constraint.

In this paper, we give theoretical estimates of the performance gain with voltage bias for several bolometers that have been reported in the literature. We find cases where the sensitivity can be greatly improved (by changing the thermal conductance) while holding the time constant fixed and others where the bolometer can be made much faster while maintaining the sensitivity.

Operationally, the change in sensor current from the voltage-biased superconducting bolometer (VSB) can be read out with a high-T<sub>c</sub> superconducting quantum interference device (SQUID) ammeter or transistor-based transimpedance amplifier. The lead resistance must be kept much lower than the bolometer resistance to maintain the constant-voltage bias.

### II. VSB THEORY

The VSB theory and operation discussed in this section and section III are applicable to both lowand high-T<sub>c</sub> bolometers. The strength of electrothermal feedback for bolometers with resistive thermometers is controlled by the quantity

 $\mathcal{L}=P_b\alpha/GT$  which is analogous to the loop gain in control circuits. Here  $P_b$  is the power dissipated in the bolometer by the bias and  $\alpha=dlogR/dlogT$  is a dimensionless measure of the steepness of the superconducting transition which can be  $10^2$  to  $10^3$  for high quality films. The electrothermal feedback is negative with the VSB and  $\mathcal{L}$  can be >>1. For a current biased superconductor,  $\mathcal{L}$  is limited to values <1 to avoid thermal instability. The current responsivity, defined as the ratio of changes in sensor current to those in absorbed optical power of the bolometer, can be computed from energy conservation[8] to give

$$S_I = -\frac{1}{V_b} \frac{\mathcal{L}}{1 + i\omega \tau_0 + \mathcal{L}}.$$
 (1)

Here,  $\omega$  is the modulation frequency of the infrared signal,  $\tau_0$ =C/G is the intrinsic thermal time constant without feedback and C is the heat capacity of the bolometer. Two features of the VSB are immediately apparent from this expression. In the limit  $\mathcal{L}>>1$ , S<sub>I</sub>=-1/V<sub>b</sub> for  $\omega<<1/\tau$ , where  $\tau$  is the VSB response time. Consequently, this bolometer has excellent linearity and is easily calibrated. Also, the Lorentzian roll-off of the responsivity occurs when  $\omega\tau_0\sim1+\mathcal{L}$  which can be >>1. Thus the negative feedback increases the speed of response with

$$\tau = \tau_0 \frac{1}{1 + \mathscr{S}}.\tag{2}$$

It should be mentioned that the  $\mathcal{L}$  term in the denominator of Eqn. 1 arises from the bias heating term in the energy conservation equation[8], so can be identified with the electrothermal feedback.

The noise equivalent power (NEP) for a VSB with  $\omega <<1/\tau$  can be written[5]

$$NEP^{2} = NEP_{photon}^{2} + \gamma 4kT^{2}G$$

$$+ \frac{1}{S_{I}^{2}} \left( i_{n}^{2} + \frac{1}{\left(1 + \mathcal{L}\right)^{2}} \left( \frac{4kT}{R} + a(\omega) \left( \frac{V_{b}}{R} \right)^{2} \right) \right), \quad (3)$$

where the terms describe statistical photon noise, thermal fluctuation noise, readout noise, Johnson noise, and excess low-frequency (often 1/f) sensor noise respectively. Here,  $i_n$  is the readout current

noise, R is the resistance of the sensor, and  $\gamma$  describes the reduction of thermal fluctuation noise due to the temperature difference between the sensor and the heat sink. The  $1/(1+\mathcal{L})$  term in Eqn. 2 describes the suppression of Johnson and low-frequency noise current by ETF first noted by Mather.[5] The low-frequency noise current is assumed to be proportional to  $V_b$ . This dependence is characteristic of both low- $T_c[9,10]$  and high- $T_c[4]$  films. Note that  $a(\omega)$  has units of inverse frequency and can depend on film geometry, film quality, and  $\alpha$ .

The NEP can be rewritten as

$$NEP^{2} = NEP_{photon}^{2} + \gamma 4kT^{2}G$$

$$+ i_{n}^{2} V_{b}^{2} + \frac{4kT^{3}G^{2}}{P_{c}\alpha^{2}} + a(\omega)\frac{G^{2}T^{2}}{\alpha^{2}}.$$
(4)

The Johnson noise contribution to the NEP depends inversely on Pb and is therefore much lower for voltage bias, where Pb can be large, than for current bias. The dependence of the lowfrequency noise on bias power depends on the model, but is independent of bias, for example, in the case of resistance fluctuations which are lowfor both and sensors.[4,9,10] The NEP for high-T<sub>c</sub> bolometers is often dominated by either the thermal fluctuation or the low-frequency noise term. In either case, the minimum NEP is obtained for a small value of G, giving a significant temperature rise. The optimum temperature rise depends on the materials that make up the thermal conductance, but can be as large as the bath temperature.[8,11] Such a large temperature rise is not possible with YBCO thermometers cooled with liquid nitrogen. For this case, the best sensitivity is obtained if G is chosen to give a temperature rise close to the maximum of ~10K.

#### III. VSB OPERATION

A representative bias and SQUID readout circuit is shown in fig. 1.[6,8] The input coil of the dc-SQUID is in series with the sensor and the voltage bias is in parallel with the SQUID-sensor combination. Constant voltage bias is obtained by current-biasing a shunt resistor, whose resistance is <<R.

The criterion that the NEP from readout noise be less than the NEP from thermal fluctuations sets a

requirement on the resistance of the bolometer. For a  $25\mu\phi_0/\sqrt{Hz}$  SQUID with a  $0.2\mu A/\phi_0$  coupling coil[12] and T=90K, R must be  $<1k\Omega$ . For large scale arrays, it may be more practical to use a transistor-based transimpedance amplifier. Given an input transistor with 3 nV/ $\sqrt{Hz}$  noise and T=90K, R must be  $>100\Omega$  for thermal fluctuation noise to dominate readout noise.

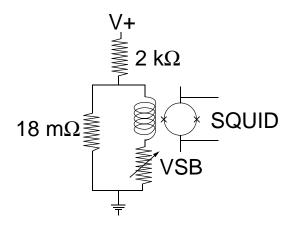


Fig. 1. Bolometer bias and SQUID readout circuit. Constant voltage bias is provided by a current biased resistor in parallel with series combination of bolometer and SQUID input coil.

The G of the VSB must be chosen to match the largest estimated value of optical loading P.[8] For a given G, the bias power is at its maximum value  $P_{b\text{-max}}$  when the optical load is negligible. As P is increased,  $P_b$  decreases. For  $\mathcal{L}>>1$ ,  $P+P_b$  is held constant and the responsivity  $S_{I}=-1/V_b$  is constant. The sensor saturates when P approaches  $P_{b\text{-max}}$ . As with many bolometers, dynamic range can be traded for sensitivity. With  $P_{b\text{-max}}=2$  x estimated P,  $P_b=P$  when P is the estimated value, and the VSB saturates when P is twice the estimated value.

The leads to the bolometer need not be superconducting, but the lead resistance must be kept much lower than the bolometer resistance to maintain the constant-voltage bias.

# IV. HIGH-T<sub>c</sub> BOLOMETER COMPARISON

In order to illustrate the importance of voltage bias for practical devices, we compare in Table I the time-constant of published (current biased) bolometers to the estimated time-constant of the same bolometers if constant-voltage bias and current readout were implemented.

The bolometers listed are from Verghese *et al.* [1], Johnson *et al.* [13], and Berkowitz *et al.* [14].

The  $\mathcal L$  values were calculated using the published transitions, assuming operation at ~10% of the normal resistance. The estimated time-constant for the VSB was then calculated using Eqn. 2. The speedup achieved in all three cases is more than one order of magnitude. The calculation of the time-constants was done under the assumption that the internal time-constant of the bolometer is short enough to not degrade the performance of the VSB. It should also be noted that the resistance of the bolometer of Johnson  $et\ al.$  would have to be reduced to satisfy the criterion for a low NEP due to readout noise given in section III. The information in the first eight rows were obtained from the references.

TABLE I COMPARISON OF PUBLISHED HIGH-Tc BOLOMETERS

	UCB/	Honeywell/	Conductus/
	Conductus	JPL	NIST
	(Verghese	(Johnson	(Berkowitz
	et al., 1993)	et al., 1994)	et al., 1996)
λ (μm)	20<λ<100	3<λ<22	12<λ<36
A (μmxμm)	$10^3 \text{x} 10^3$	140x105	50x50
P (W)	-	3.4x10 <sup>-7</sup>	-
G (W/K)	2.7x10 <sup>-4</sup>	8.5x10 <sup>-8</sup>	8x10 <sup>-7</sup>
C (J/K)	1.5x10 <sup>-5</sup>	6.7x10 <sup>-9</sup>	1x10 <sup>-9</sup>
τ (Ibias)(ms)	55	105	1.2
NEPtherm $(W/\sqrt{Hz})$	1.1x10 <sup>-11</sup>	2x10 <sup>-13</sup>	6x10 <sup>-13</sup>
NEP	2.4x10 <sup>-11</sup>	1.5x10 <sup>-12</sup>	1.2x10 <sup>-12</sup>
(W/√Hz)	@10Hz	@2Hz	@32Hz
$\mathscr{L}$ (VSB)	29	12	27
τ(VSB)(ms)	2	6	0.045

It is of interest to consider how these bolometers should be re-optimized to take full advantage of the voltage bias for specific applications. In this illustration, we assume that the value of G can be changed as required. In practice, such changes may not be straightforward.

The Verghese *et al.* device is a composite bolometer designed for use with a far infrared step-and-integrate laboratory Fourier spectrometer. For this application, G could be decreased by an order of magnitude with voltage bias while holding the response time roughly constant. Since the contributions to the NEP due to thermal fluctuations and low-frequency noise scale as  $\sqrt{G}$  and G, respectively (see Eqn. 4), the NEP should be decreased by more than a factor of  $\sim$ 3.

Alternatively, the frequency response could be extended to 1kHz to allow this bolometer to be

used with a laboratory rapid-scan Fourier spectrometer for measurements throughout the infrared. The required  $G=3x10^{-3}$  would be well matched to the combination of a 900K source and a throughput of  $10^{-2}$  cm<sup>2</sup>-sr. The NEP is then estimated to be  $\sim 4x10^{-11}$ .

The bolometer of Johnson *et al.* is a monolithic device designed for array imaging. The G of the Johnson *et al.* device is close to optimal for thermal imaging, but the time-constant is long for an imaging camera. Voltage bias would give a very useful camera frame rate of ~30Hz, with the same value of G. The contribution to the NEP from the low-frequency noise would also be reduced since the device would be operated at a higher frequency. If the NEP<sup>2</sup> scales as 1/f, then the NEP would decrease by a factor of four.

The bolometer of Berkowitz *et al.* is also a monolithic device designed for array imaging. The G of the Berkowitz *et al.* device is larger than optimal for thermal imaging, but the device speed is adequate for a 30 Hz camera frame rate. With voltage bias, it would be desirable to reduce G up to an order of magnitude (depending on the optical loading) giving a factor ~3 decrease in NEP, while retaining the bandwidth of the device.

# V. CONCLUSION

We have described a potential major improvement in high- $T_c$  bolometer technology. The time-constant decrease of the VSB results in a powerful combination of speed and sensitivity. Many of the applications of high- $T_c$  bolometers have a strict time-constant requirement, and given that constraint the use of voltage bias results in a substantial increase in sensitivity for the current generation of devices.

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